Immune PID controller based on differential evolution algorithm for heart rate regulation

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Abstract
This paper presents different structures of immune proportional-integral-derivative (PID) control system, to regulate the heart rate. It is based on Yanagihara, Noma, and Irisawa (YNI) model that represent the mathematical model of the heart. Three structure designs have been proposed to emphasize the optimality in the control process. In this work differential evolution (DE) algorithm is considered to optimize the controller parameters. The performance of the proposed three controllers has been compared to traditional PID methods. The comparison results show best improvement when using the proposed structure-III with 0% maximum overshoot, a reduction of 98.9%, 96.8% and 30.8% in rising time, settling time, and steady state error respectively.

Keywords
Immune system, Proportional-integral-derivative (PID) controller, Differential evolution, Human heart, YNI model.

1. Introduction
Cardiovascular diseases constitute the major causes of death worldwide, especially in the developed countries. Two famous cardiac diseases are bradycardia and tachycardia, which results in shortness of breath, fainting and in sometimes death [1, 2]. Bradycardia is defined as a heart rate less than 60 bpm. Its symptoms become clear when the rate drops below 50 bpm, while tachycardia is defined as a heart rate greater than 120 bpm [3]. There are various solutions to treat heart diseases, from the simplest, such as diet to sophisticated solutions such as heart transplantation. The fast development in technology offers a solution in between, which is more efficient than the diet, yet less risky than heart transplantation. This can be achieved by using an electronic device that observes heart functionality and compensate any disorder. In the last years, several researchers developed the control system to regulate the heartbeat like fractional-order PID (FOPID) controller which is suggested by Arunachalam et al. [4] for cardiac pacemaker based on the Ziegler-Nichols tuning method.

The result was found that, the FOPID controller was better in terms of overshoot, settling time, and rising time than comparative controller. Aabid et al. [5] use PID controller, which its coefficients are tuned by ant colony optimization (ACO) algorithm in order to control and improve the hydro-electromechanical (HEM) mathematical model of the human heart that based on YNI model. Aghdam et al. [6] suggest a new intelligent control algorithm using adaptive neuro-fuzzy inference system (ANFIS) for cardiac pacemakers based on various states of patient blood pressure, sex, and age; various states of the body exercising, walking, and the rest. Karar [7] developed a new adaptive backstepping control based on radial basis function to improve the performance of dual sensor pacemakers to regulate heart rate. He tested the suggested controller by using pre-determined data for different patients heart rate [7]. Castroa and Malathi [8] designed a backpropagation neural network (BPNN) based on the conventional PID controller, to regulate the heart rate. The coefficients of a PID tuned by Zeigler-Nichols represents the weights of the output layer in BPNN. Elnaggar et al. [9] designed a fuzzy-proportional–derivative (FPD) controller of a cardiac pacemaker. The fuzzy controller, which is Mamdani type considered as an integration in a conventional PID.

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In this paper, the concept of the body's immune system as a controller with PID is used to regulate the arrhythmia that happened in heart rate, based on the DE to tune its parameters. To achieve these goals, since the 1960s, different mathematical models of the human heart have been investigated using the physical models of real systems as reference scales [10]. One of them is the YNI model which considered here.

The rest of this paper is outlined as follows: section 2 presents the mathematical model of a heart. Section 3 describes the immune system details, while section 4 illustrates the DE algorithm. Section 5 explains the design of proposed immune-PID structures controller. Section 6 addresses the simulation results and analysis of the proposed controllers, and section 7 provides the final conclusion.

2. Mathematical model of a heart

There are different mathematical models that represent the human heart, such as Nobel model [11] which presents a representation of the Purkinje fiber cell's action potential. Mcallister, Noble, and Tsien (MNT) model offers an improved model for the Purkinje fiber's action potential [12]. Beeler and Reuter [13] present the first model of ventricular myocardial cell's electrical behaviour. The YNI model is one of the earliest models of Sino Atrial (SA) nodal cell's action potential behaviour [2, 14, 15]. All these models are of Hodgkin–Huxley (HH) type, which expressed in terms of ionic currents and conductance.

In this paper, the SA model is used to represent the mathematical model of the human heart. The YNI model can simulate the heart's action potentials accurately. YNI model is an HH type, which is based on voltage clamp data. Where the relationship between voltage and current is considered and simulates the spontaneous action potential. The YNI model has four types of time-dependent currents (delayed inward current activated by hyperpolarization \( I_h \), slow inward current \( I_s \), potassium current \( I_k \), and sodium current \( I_{Na} \)), and one time-independent current is the leakage current \( I_l \).

The equivalent electrical circuit model of a cell membrane can be represented by a capacitor and variable resistor as stated in [15].

The unit of the trans-membrane current is \( \mu A/cm^2 \).

\[
C_m \frac{dV}{dt} + I_h + I_s + I_l + I_{Na} = I_{app} \tag{1}
\]

Where \( C_m \) is a constant (\( \mu F/cm^2 \)) refers to the cell membrane capacitance; \( I_{app} \) represents the external applied current.

The Equation 1 can be simplified as:

\[
C_m \frac{dV}{dt} + I_{ion} = C_m \frac{dV}{dt} + C_m \frac{V}{R_m} = I_{app} \tag{2}
\]

Where \( C_m \) and \( R_m \) represent the capacitance and the resistance respectively of the cell membrane.

Where

\[
I_h = 0.4q(V + 45) \tag{3}
\]

\[
I_s = 12.5 \left( 0.05 + 0.95d \right) \left( 0.05 + 0.95f \right) \left( \exp \frac{V + 40}{20} - 1 \right) \tag{4}
\]

\[
I_l = 0.8 \left( 1 - \exp \frac{V + 60}{20} \right) \tag{5}
\]

\[
I_k = 0.7p \frac{\exp \left( 0.0277(V+90) \right) - 1}{\exp \left( 0.0277(V+40) \right)} \tag{6}
\]

\[
I_{Na} = 0.5m^2h(V - 30) \tag{7}
\]

\[
\frac{dw}{dt} = \alpha_w(1 - w) - \beta_w w \tag{8}
\]

Where \( w = \{ q, d, f, p, m, \text{ or } h \} \).

The gating variables \( q, d, f, p, m, \text{ and } h \) must satisfy the first-order differential Equation 8. Using the constants' values listed in Table 1, constants \( \alpha_w \) and \( \beta_w \) can be obtained as shown in Equation 9.

\[
\alpha_w, \beta_w = \frac{c_4 \exp \left( \frac{V - V_0}{C_2} \right) - c_5 \exp \left( \frac{V - V_0}{C_3} \right)}{1 + c_4 \exp \left( \frac{V - V_0}{C_2} \right)} \tag{9}
\]

The parameters \( \alpha_p, \alpha_q, \beta_q, \alpha_d, \beta_d \) cannot be calculated from Equation 9, therefore, they are calculated by:

\[
\alpha_p = 9 \times 10^{-3} \frac{1}{1 + \exp \left( \frac{V + 40}{9.71} \right)} + 6 \times 10^{-4} \tag{10}
\]

\[
\alpha_q = 3.4 \times 10^{-4} \frac{\exp \left( \frac{V + 40}{4.4} \right) - 1}{\exp \left( \frac{V + 150}{4.4} \right) - 1} + 4.95 \times 10^{-5} \tag{11}
\]

\[
\beta_q = 5 \times 10^{-4} \frac{1 - \exp \left( - \frac{V + 40}{6} \right)}{1 - \exp \left( - \frac{V + 40}{35} \right)} + 8.45 \times 10^{-5} \tag{12}
\]

\[
\alpha_d = 1.045 \times 10^{-2} \frac{\exp \left( - \frac{V + 35}{2.5} \right) - 1}{\exp \left( - \frac{V + 35}{2.5} \right) + 3.125 \times 10^{-2}} \tag{13}
\]

\[
\beta_d = 9.44 \times 10^{-4} \frac{(V + 60)}{1 - \exp \left( - \frac{V + 60}{4.16} \right)} \tag{14}
\]
4. Differential evolution algorithm

DE is one of the most popular optimisation techniques, which modifies iteratively a population of candidate solutions to make it converge to an optimum solution. The right immune response must be stable and has fast reaction to remove all attacking antigens. In addition, a high antibody consistency must be controlled since it may harm the body. In a control system of dynamic regulation, the deviation must be linked to ensure the ability of the immune system. As an adaptive and self-tuning approach, DE algorithm is applied to random differential (scaling factor), and then the B-cell produces corresponding antibodies to resist the antigen with the stimulation of the Tα and Tβ, [16]. When the cell obtains the antigen, it transmits the information to the B-cells consistency and the antigen, can be written as the following:

\[
T_0 (t) = F (k \alpha (k - d) - \beta) e^{- \beta t} + \alpha
\]

(18)

Table 1: Defined values of \( \beta \) and \( \alpha \) of YNI model [15]

<table>
<thead>
<tr>
<th>( \beta )</th>
<th>( \alpha )</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.1</td>
<td>0.1</td>
</tr>
<tr>
<td>0.2</td>
<td>0.2</td>
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<tr>
<td>0.3</td>
<td>0.3</td>
</tr>
<tr>
<td>0.4</td>
<td>0.4</td>
</tr>
</tbody>
</table>

5. Conclusion

A natural immune system is a detection system distributed throughout the body with many functional components in strategic positions. Identifying all antigens and tissues, the body learns to recognize the foreign antigens (such as viruses or bacteria) from the cells or molecules of the body. The proper type of immune cells is the lymphocyte, which forms the immune response, and includes adaptability, specificity, the attributes of diversity and memory. The main two types of lymphocytes are the B-cells and the T-cells. The B-cells, which produce antibodies, to resist the antigen with the stimulation of the Tα and Tβ, [16]. When the cell obtains the antigen, it transmits the information to the B-cells consistency and the antigen, can be written as the following:

\[
T_0 (t) = F (k \alpha (k - d) - \beta) e^{- \beta t} + \alpha
\]

(18)

The right immune response must be stable and has fast reaction to remove all attacking antigens. In addition, a high antibody consistency must be controlled since it may harm the body. In a control system of dynamic regulation, the deviation must be linked to ensure the ability of the immune system. As an adaptive and self-tuning approach, DE algorithm is applied to random differential (scaling factor), and then the B-cell produces corresponding antibodies to resist the antigen with the stimulation of the Tα and Tβ, [16]. When the cell obtains the antigen, it transmits the information to the B-cells consistency and the antigen, can be written as the following:

\[
T_0 (t) = F (k \alpha (k - d) - \beta) e^{- \beta t} + \alpha
\]

(18)
Step 4: keep the better solution \((U_j \text{ or } X_j)\)
end for
end for

Assume the error \(e(k)\) referred to the amount of antigen \(\delta(k)\), and the input of the controller \(u(k)\) will be the total motivation that is accepted by the B-cells. Then the feedback control system will be represented as:
\[
u(k) = K \{1 - \eta f[\Delta u(k - d)]\} e(k) = K_f e(k)
\]  \hspace{1cm} (19)

Where \((1 - \eta f[\Delta u(k - d)]) = K_f\) is the immune controller's proportional gain, \(\eta = \frac{K_2}{K_3}\) is the gene that controls the amount of \(K_f\), and \(f\) is a nonlinear function.

A nonlinear function is selected here as T-cell's regulate action-function, dependent on the influence of the antigen consistency on antibody in immune response.
\[
f(x) = 1 - \frac{1}{1 + \exp(-cx)} \quad c > 0,
\]  \hspace{1cm} (20)

Where the range of \(f(x)\) is \([-1, 1]\), the active region of \(x\) is determined by \(c\) value.

It can be written the immune controller's output as:
\[
u(k) = K \left\{1 - \eta \left(1 - \frac{2}{1 + \exp(-cx)}\right)\right\} e(k) = K_f e(k)
\]  \hspace{1cm} (21)

Figure 1 DE algorithm

5. Proposed algorithm

In this paper three structures of Immune-PID controller is proposed to regulate the case of the arrhythmia. The parameters of the PID and Immune blocks are tuned using the DE algorithm. The three structures are explained in following subsections.

5.1 Immune PID structure I

Figure 2 The immune PID controller block diagram structure I
5.2 Immune PID structure II

The block diagram of this structure is shown in Figure 3, where the PID is connected in parallel with the immune controller and the input for PID and immune controller is the error signal \( e(k) \). The control law for this structure is:

\[
u(k) = k_i e(k) + k_p \left[ 1 + \frac{k_i}{1-z^{-1}} + k_d (1-z^{-1}) \right] e(k)
\] (23)

![Figure 3 The immune PID controller block diagram structure II](image)

5.3 Immune PID structure III

Figure 4 illustrate the block diagram for this structure, where the PID is multiplied by the immune controller and the error signal is consider as input signal for these two controllers. The control law for this structure is:

\[
 u(k) = k_i e(k) \times k_p \left[ 1 + \frac{k_i}{1-z^{-1}} + k_d (1-z^{-1}) \right] e(k).
\] (24)

![Figure 4 The immune PID controller block diagram structure III](image)

6. Simulation results and analysis

The simulation results of the proposed controllers based on the DE algorithm for controlling YNI heart rate model have been presented in this section for the heart rate of 60 bpm (older person) and 70 bpm (normal adult). The YNI model response to the two cases without controller is shown in Figure 5 and Figure 6 respectively. These results show that the actual (output) heart rate has reached the desired rate very fast (small settling time \( t_s \)) but there is an error in the steady state in both cases (60 bpm and 70 bpm). Therefore the proposed controller is used based on DE algorithm.

The DE algorithm parameters are considered here are listed in Table 2. The optimal controller parameters for classical discrete PID and immune-PID structures obtained by the DE algorithm are listed in Table 3.
Figure 5 The YNI response for heart rate (HR) =60 bpm

Figure 6 The YNI response for heart rate (HR) =70 bpm

Table 2 The parameters that are used in DE algorithm

<table>
<thead>
<tr>
<th>DE parameters</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of tuned parameters (D)</td>
<td>5</td>
</tr>
<tr>
<td>Population size (NP)</td>
<td>15</td>
</tr>
<tr>
<td>Crossover constant (CR)</td>
<td>0.6</td>
</tr>
<tr>
<td>Mutation constant (F)</td>
<td>0.85</td>
</tr>
<tr>
<td>Number of generations (GEN)</td>
<td>20</td>
</tr>
</tbody>
</table>

Table 3 Optimal controller parameters

<table>
<thead>
<tr>
<th>Controller</th>
<th>$k_p$</th>
<th>$k_i$</th>
<th>$k_d$</th>
<th>$K_i$</th>
<th>$\eta$</th>
<th>$\epsilon$</th>
</tr>
</thead>
<tbody>
<tr>
<td>PID</td>
<td>3.6080</td>
<td>6.6867</td>
<td>0.0026</td>
<td>---</td>
<td>---</td>
<td>---</td>
</tr>
<tr>
<td>Immune-PID1</td>
<td>2.6781</td>
<td>7.2447</td>
<td>0.000299</td>
<td>9.6190</td>
<td>0.4634</td>
<td>0.5</td>
</tr>
<tr>
<td>Immune-PID2</td>
<td>5.2337</td>
<td>8.8503</td>
<td>0.0039</td>
<td>4.1499</td>
<td>0.0156</td>
<td>0.5</td>
</tr>
<tr>
<td>Immune-PID3</td>
<td>2.3853</td>
<td>9.0849</td>
<td>0.000012</td>
<td>9.354</td>
<td>0.6066</td>
<td>0.5</td>
</tr>
</tbody>
</table>

The simulation response of YNI model after regulated it by the proposed controllers (immune PID with three structures) in addition to optimal PID (which also tuned by the DE algorithm as illustrated in Table 3) are shown in Figure 7 and Figure 8 respectively.

It can be noticed from Figure 7 and Figure 8 that all the controller satisfies the design requirement by making the cardiac system follows the desired heart rate with small steady state error ($e_{s.s}$), settling time ($t_s$), rise time ($t_r$) and overshoot ($M_p$) as shown in Table 4 and Table 5 especially immune-PID structure III which has best average performance than the optimal PID, immune-PID structure I, and immune-PID structure I).
Table 4 and Table 5 also illustrate that the performance of the immune-PID-structure II is nearly similar to the performance of immune-PID-structure III as compared to immune-PID-structure II and optimal PID.

### Table 4 The evaluation parameters of simulation results for HR=60 bpm

<table>
<thead>
<tr>
<th>Controller type</th>
<th>Mp (%)</th>
<th>t_r (sec)</th>
<th>t_s (sec)</th>
<th>ε Ass</th>
</tr>
</thead>
<tbody>
<tr>
<td>PID</td>
<td>0.92</td>
<td>0.031</td>
<td>0.0482</td>
<td>-0.32</td>
</tr>
<tr>
<td>Immune-PID Structure I</td>
<td>0.354</td>
<td>0.0047</td>
<td>0.0081</td>
<td>-0.065</td>
</tr>
<tr>
<td>Immune-PID Structure II</td>
<td>0.315</td>
<td>0.0126</td>
<td>0.022</td>
<td>0.31</td>
</tr>
<tr>
<td>Immune-PID Structure III</td>
<td>0</td>
<td>0.00034</td>
<td>0.0019</td>
<td>0.26</td>
</tr>
</tbody>
</table>

### Table 5 The evaluation parameters of simulation results for HR=70 bpm

<table>
<thead>
<tr>
<th>Controller type</th>
<th>Mp (%)</th>
<th>t_r (sec)</th>
<th>t_s (sec)</th>
<th>ε Ass</th>
</tr>
</thead>
<tbody>
<tr>
<td>PID</td>
<td>1.68</td>
<td>0.0284</td>
<td>0.0477</td>
<td>0.39</td>
</tr>
<tr>
<td>Immune-PID Structure I</td>
<td>0.486</td>
<td>0.0048</td>
<td>0.008</td>
<td>0.04</td>
</tr>
<tr>
<td>Immune-PID Structure II</td>
<td>0.6171</td>
<td>0.0124</td>
<td>0.0222</td>
<td>0.315</td>
</tr>
<tr>
<td>Immune-PID Structure III</td>
<td>0</td>
<td>0.00029</td>
<td>0.0015</td>
<td>0.27</td>
</tr>
</tbody>
</table>

#### 7. Conclusion

In this paper, three different structures of immune-PID controller are investigated instead of the traditional discrete PID controller to regulate the heart rate. The mathematical model of heart YNI has been considered. In order to improve the characteristics of the proposed controllers, DE algorithm have been applied. The simulation results show that the immune-PID structure III outperforms the other structures. In this structure the control action of the controller is the product of the immune controller output and the PID controller output. For
future works, we suggest implementing this controller as hardware using field programmable gate array (FPGA) and experience the suggested controller on mechanical systems such as manipulator robotic systems.

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Conflicts of interest
The authors have no conflicts of interest to declare.

References

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